# SEISMIC ANALYSIS OF A LIQUID STORAGE TANK WITH A BAFFLE 

A. Gedíklì and M. E. Ergüven<br>Technical University of Istanbul, Civil Engineering Faculty, Maslak, Istanbul 80626, Turkey

(Received 5 September 1998, and in final form 4 January 1999)

The effects of a rigid baffle on the seismic response of liquid in a rigid cylindrical tank are presented. A baffle is an additional structural element which supplies a kind of passive control on the effects of earthquake motion. Fluid motion is assumed to be irrotational, incompressible and inviscid. The method of superposition of modes has been implemented to compute the seismic response. The boundary element method is used to evaluate the natural modes of liquid in a cylindrical tank. Linearized free surface conditions have been taken into consideration.
© 1999 Academic Press

## 1. INTRODUCTION

In recent years, the civil engineering community has been concerned with the development and implementation of innovative design concepts for seismic protection of structures, particularly for the control of earthquake effects on buildings [1, 2].

Seismic response reduction systems need not be located only in the base of the structure. Control systems have mainly two categories called active and passive systems. The system is called an active control system if external forces are applied with the base isolation system to the structure to control the earthquake effects. In passive control systems external forces are not required [1].

Attempts have been made to install them in different parts of the structure, either in the form of additional response reduction masses, or dampers, friction devices, etc. One of the passive control systems is based on the known behavior of a braced steel frame when using friction effects of friction dampers. During an earthquake the friction damper mechanism develops additional energydissipating sources which can protect the main members from structural damage.

In liquid containers, breaking of surface waves, while highly dependent on vibration amplitude, is the main mechanism of energy dissipation. Liquid dampers have been in use in space satellites and marine vessels. The value of additional damping can increase with low viscosity of the liquid, with a smooth bottom of the container, and with an adequate gap between the liquid and the roof of the container. Another approach to the response reduction systems is the
coupling of individual structural systems, one alongside another with different stiffness, and intermediate energy absorbing systems.

Vondorn [3] reported the damping effect of the bottom boundary layer on liquid motion. Miles [4] also studied the ring damping of free surface oscillations in a cylindrical tank.

If stiffeners are required in the tank design for structural integrity, the baffles and support rings may serve the dual purpose of slosh damper for passive control of the tank and stiffener. Several rings can be supported around the tank periphery and positioned slightly below the liquid surface.

The phenomenon of earthquake damage on the nuclear power plants and petroleum tanks creates an important research area in the seismic analysis of liquid storage tanks [5, 6]. The behavior of the liquid in rigid tanks has been examined by some authors over a number of decades [7, 8]. Studies with flexible tank assumptions are later than those with rigid tank assumptions [9-11]. There are studies that compare different methods of seismic analysis for partially liquid filled or empty containers [12-14].

Some authors make use of a mass-spring model of the liquid [15-19], while others tend to solve the potential problems [20-22]. Perturbation expansions also have been used for calculation of the water waves [23]. A semi-analytical method uses Fourier series and FEM [24]. Numerical inversion of transformation methods [25], the panel method based on the boundary integral technique [26], the finite element method [27] and Galerkin's approach [14] have been used to solve the liquid sloshing problem in cylindrical tanks that are elastic or rigid with linear or non-linear free surface conditions. Compressibility of the liquid has been considered for the analysis of dams [28, 29].

The boundary element method can be used to evaluate the natural frequencies and the natural modes of the liquid. The technique of superposition of the modes has then been used for the seismic analyses [8, 20].

Passive systems can be configured with additional structural elements, such as mass-damper-spring systems or baffles in liquid storage tanks [30, 31].

In this study, to examine the effectiveness of baffle for liquid oscillations as passive control systems, the forces acting on the foundation of the baffle-tank system, caused by the hydrodynamic pressure of the fluid, is determined by using the boundary element method.

By choosing the suitable geometry for the baffle-tank system, the magnitudes of the forces mentioned above can be minimized for a kind of passive control system.

### 1.1. ASSUMPTIONS

The following are assumed for the liquid: (1) either the velocity or the displacement of a particle on the free surface is so small that the kinematic and the dynamic conditions can be linearized; (2) the fluid is incompressible and inviscid; (3) the fluid motion is irrotational.

The following are assumed for the baffle-tank system: (4) the baffle-tank system is a rigid structure and fixed on a rigid foundation; (5) the baffle-tank
system moves only in the horizontal direction under the effect of the recorded earthquake acceleration.

## 2. FUNDAMENTAL EQUATIONS

The cylindrical co-ordinate system $(r, \theta, z)$ for the baffle-tank system is fixed as shown in Figure 1. A Cartesian co-ordinate system is fixed at the bottom of the tank to make easy the definition of shear force and the overturning moment acting on the foundation. The relation between these two co-ordinate systems is

$$
\begin{equation*}
x=r \cos \theta \quad \text { and } \quad y=r \sin \theta \tag{1}
\end{equation*}
$$

A way to analyze the behavior of the liquid is the use of velocity potential as in references [20-22].

A non-dimensional form will be chosen because the results then become more understandable. The radius of the $\operatorname{tank} R$, the gravitational acceleration $g$ and the density of the liquid $\rho_{f}$ are used in the procedure for establishment of the non-dimensional forms [20]. Thus, one has

$$
\Phi \leftarrow \Phi \sqrt{g R^{3}} \text { (velocity potenial), } \quad p \leftarrow p / \rho_{f} g R \text { (hydrodynamic pressure), }
$$

$a \leftarrow a / g$ (recorded earthquake acceleration in $x$-direction),
$r \leftarrow r / R$ (radial component of cylindrical co-ordinate system),
$z \leftarrow z / R$ (vertical component of cylindrical co-ordinate system),
$t \leftarrow t \sqrt{g / R}$ (time), $\omega \leftarrow \omega \sqrt{R / g}$ (angular frequency),
$\eta \leftarrow \eta / R$ (vertical displacement of a particle on the free surface),
$F_{x} \leftarrow F_{x} / \rho_{f} g R^{3}$ (shear force at the bottom of the tank),
$M_{y} \leftarrow M_{y} / \rho_{f} g R^{4}$ (overturning moment around axis of $y$ ).


Figure 1. Rigid cylindrical tank with a baffle and co-ordinate systems.

Here the arrows indicate the non-dimensional terms. Shear force and overturning moment are respectively

$$
\begin{equation*}
F_{x}=\int_{S_{r}} p n_{x} \mathrm{~d} S \quad \text { and } \quad M_{y}=\int_{S_{r}}\left(z n_{x}-x n_{z}\right) p \mathrm{~d} S, \tag{3}
\end{equation*}
$$

where $n_{x}$ and $n_{z}$ are the components of the outward normal of the surface in the $x$ and $z$ directions, respectively. A harmonic boundary value problem can be represented by using the velocity potential as follows:

$$
\begin{gather*}
\nabla^{2} \Phi=0 \text { in the region of the liquid } R_{f},  \tag{4}\\
\Phi_{, n}=0 \text { on the rigid surface } S_{r},  \tag{5}\\
\Phi_{, z}=\dot{\eta} \text { kinematic condition on the free surface } S_{f s},  \tag{6}\\
\eta=\dot{\Phi}+a x \text { dynamic condition on the free surface } S_{f s} . \tag{7}
\end{gather*}
$$

Here $a(t)$ is the recorded earthquake acceleration and a superposed dot implies time differentiation. A comma followed by a subscript indicates partial differentiation with respect to the corresponding spatial variable. Initial conditions are as follows: at $t=0$

$$
\begin{equation*}
\Phi=0 \text { in } R_{f}, \quad \dot{\Phi}=0 \text { in } R_{f} . \tag{8,9}
\end{equation*}
$$

The hydrodynamic pressure of the liquid can be written as

$$
\begin{equation*}
p=-\dot{\Phi}-a x \quad \text { in } \quad R_{f}+S_{r} . \tag{10}
\end{equation*}
$$

The meaning of the kinematic condition is that a particle on the free surface will always stay on the free surface and that of the dynamic condition is that pressure on the free surface is zero. A linear dynamic condition can be obtained by the use of Bernoulli's equation in the case of low velocities. Substituting equation (6) into equation yields (7) a linear free surface condition as

$$
\begin{equation*}
\Phi_{, z}=\ddot{\Phi}+\dot{a} x \quad \text { on } \quad S_{f s} . \tag{11}
\end{equation*}
$$

### 2.1. SUPERPOSITION OF MODES

The velocity potential field of the liquid in the cylindrical tank can be written in the form

$$
\begin{equation*}
\Phi(r, \theta, z, t)=\sum_{k=0}^{\infty} \cos k \theta \sum_{n=1}^{\infty} \phi_{n}(r, z) \psi_{k n}(t), \tag{12}
\end{equation*}
$$

where $\phi_{n}$ is the value of the velocity potential on the plane of $\theta=0$ and $\psi_{k n}$ is the weighting factor. $k$ and $n$ are the numbers for the modes in the circumferential and radial directions, respectively. Cases $k=0$ and $k=1$ correspond to axially
symmetric and asymmetric mode shapes, respectively. In this paper, for the sake of simplicity and sufficiency, only the term $k=1$ has been used, so omitting index $k$ from equation (12) one has

$$
\begin{equation*}
\Phi(\theta, z, t)=\cos \theta \sum_{n=1}^{\infty} \phi_{n}(r, z) \psi_{n}(t) . \tag{13}
\end{equation*}
$$

For the modes of natural vibration, by taking $\psi_{n}(t)=\sin \omega_{n} t$ and $a(t)=0$ then substituting equation (13) into equation (11), the following condition for the $n$th mode is obtained:

$$
\begin{equation*}
\phi_{n, z}=-\omega_{n}^{2} \phi_{n} . \tag{14}
\end{equation*}
$$

Here $\omega_{n}$, is the natural frequency of the $n$th mode. The velocity potential field for the liquid under the effect of the recorded earthquake acceleration can be evaluated by the use of mode shapes and natural frequencies of natural vibration. Substituting equations (13) and (14) into equation (11) yields the following form for the function $\psi_{n}$ :

$$
\begin{equation*}
\sum_{n=1}^{\infty}\left(\ddot{\psi}+\omega_{n}^{2} \psi_{n}\right) \phi_{n}=-\dot{a} r \quad \text { on } \quad S_{f s} . \tag{15}
\end{equation*}
$$

By the use of the orthogonality of the mode shapes of the velocity potential [20], the following form can be obtained from equation(15):

$$
\begin{equation*}
\ddot{\psi}_{n}(t)+\omega_{n}^{2} \psi_{n}(t)=-I_{n} \dot{a} . \tag{16}
\end{equation*}
$$

Here

$$
\begin{equation*}
I_{n}=\int_{\Gamma_{f s}} r^{2} \phi_{n} \mathrm{~d} s / \int_{\Gamma_{s s}} r \phi_{n}^{2} \mathrm{~d} s, \tag{17}
\end{equation*}
$$

where $\Gamma_{f s}$ is the intersection of $S_{f s}$ and the $\theta=0$ plane (see Figure 2). The solution of equation (16) satisfying the initial conditions (8) and (9) is Duhamel's integral

$$
\begin{equation*}
\psi_{n}(t)=-\frac{I_{n}}{\omega_{n}} \int_{0}^{t} \dot{a}(\tau) \sin \left[\omega_{n}(t-\tau)\right] \mathrm{d} \tau . \tag{18}
\end{equation*}
$$

By partial integration of equation (18) with respect to time

$$
\begin{equation*}
\psi_{n}(t)=-I_{n} \int_{0}^{t} a(\tau) \cos \left[\omega_{n}(t-\tau)\right] \mathrm{d} \tau \tag{19}
\end{equation*}
$$

is obtained, where $a(0)=0$. A numerical integration of equation (19) is easier than that of equation (18). Duhamel's integral (19) has been numerically evaluated by using the trapezoidal integration rule.


Figure 2. $\theta=0$ plane. (a) Cylindrical tank; (b) cylindrical tank with a baffle.

## 3. BOUNDARY ELEMENT METHOD

The boundary integral equation form of equation (4) can be written for any mode shape of the velocity potential, upon omitting index $n$ as [32]

$$
\begin{equation*}
-\alpha_{P} \phi(P)=\int_{\Gamma}\left\{\phi \frac{\partial G^{*}}{\partial n}-G^{*} \frac{\partial \phi}{\partial n}\right\} r \mathrm{~d} s \tag{20}
\end{equation*}
$$

Here $G^{*}$ is the free space Green function for the axially-asymmetric problem ( $\cos \theta$ type). $\alpha_{P}$ is defined by the position of the source point $P$ as

$$
\alpha_{P}=\left\{\begin{array}{cc}
4 \pi & P \in R_{f}  \tag{21}\\
2 \pi & P \in S_{f} \\
0 & P \notin R_{f}+S_{f}
\end{array}\right\}
$$

The boundary element method with the constant elements is used for the solution of the initial value problem. By evaluating the integrals in equation (20) over constant boundary elements by using the shown source position in Figure 3, the following linear system of equations is obtained [33]:

$$
\begin{equation*}
-\alpha_{P} \phi(P)=H_{i k} \phi_{k}-G_{i k} \phi_{k, n}, \quad k=1,2, \ldots N \quad \text { and } \quad i=1,2, \ldots N \tag{22}
\end{equation*}
$$

Here the source point is near to the $i$ th element and the boundary integral is evaluated over the $k$ th element (see Figure 3). $\phi_{k}$ is the value of the velocity potential of the $k$ th element. $H_{i k}$ and $G_{i k}$ are the boundary integrals given by

$$
\begin{equation*}
H_{i k}=\int_{\Gamma_{k}} G_{i, n}^{*}(P, s) r(s) \mathrm{d} s, \quad G_{i k}=\int_{\Gamma_{k}} G_{i}^{*}(P, s) r(s) \mathrm{d} s \tag{23,24}
\end{equation*}
$$

where $G_{i}^{*}(P, s)$ is called the free space Green function which is the potential on the point $s$ due to the unit source located on point $P$. For the axially-asymmetric problem ( $\cos \theta$ type), one has


Figure 3. Constant boundary elements on the $\theta=0$ plane and source point position.

$$
\begin{equation*}
G_{i}^{*}(P, s)=\frac{4}{r_{P s}}\left\{\left(\frac{2}{\kappa^{2}}-1\right) \mathrm{K}(\kappa)-\frac{2}{\kappa^{2}} \mathrm{E}(\kappa)\right\} \tag{25}
\end{equation*}
$$

and the outward normal component of the velocity of liquid particles on the boundary for this potential field is [32]

$$
\begin{align*}
G_{i, n}^{*}(P, s)= & \frac{4}{r_{P s}}\left\{\left[r_{P}\left(\frac{2}{\kappa^{2}}-1\right)-r_{s}\right] n_{r}+\left(z_{P}-z_{s}\right) n_{z}\right\} x \\
& \times\left\{\frac{1}{1-\kappa^{2}}\left(\frac{2}{\kappa^{2}}-1\right) \mathrm{E}(\kappa)-\frac{2}{\kappa^{2}} \mathrm{~K}(\kappa)\right\}-\frac{1}{2} G_{i}^{*}(P, s) n_{r} \tag{26}
\end{align*}
$$

where $\kappa=4 r_{P} r_{s} / r_{P s}^{2}$ and $r_{P s}^{2}=\left(r_{P}+r_{s}\right)^{2}+\left(z_{P}-z_{s}\right)^{2} . n_{r}$ and $n_{z}$ are the components in the radial and vertical directions, respectively. $\mathrm{K}(\kappa)$ and $\mathrm{E}(\kappa)$ are the first and secod kind complete elliptic integrals, respectively [32].

A logarithmic singularity in $\mathrm{K}(\kappa)$ occurs when the source point $P$ is located on the $i$ th element, i.e., $\kappa \rightarrow 0$. In order to avoid a singularity, the source point may be located out of the liquid domain near to the boundary.

Let $f, r$ and $c$ indices denote the parts of the liquid's surface that are free, rigid and the interface of the liquid domains, respectively. By using these indices and equation (5), the system of equations (22) can be written as

$$
\left[\begin{array}{lll}
\mathbf{H}_{f f} & \mathbf{H}_{f r} & \mathbf{H}_{f c}  \tag{27}\\
\mathbf{H}_{r f} & \mathbf{H}_{r r} & \mathbf{H}_{r c} \\
\mathbf{H}_{c f} & \mathbf{H}_{c r} & \mathbf{H}_{c c}
\end{array}\right]\left\{\begin{array}{l}
\boldsymbol{\phi}_{f} \\
\boldsymbol{\phi}_{r} \\
\boldsymbol{\phi}_{c}
\end{array}\right\}=\left[\begin{array}{lll}
\mathbf{G}_{f f} & \mathbf{G}_{f r} & \mathbf{G}_{f c} \\
\mathbf{G}_{r f} & \mathbf{G}_{r r} & \mathbf{G}_{r c} \\
\mathbf{G}_{c f} & \mathbf{G}_{c r} & \mathbf{G}_{c c}
\end{array}\right]\left\{\begin{array}{c}
\mathbf{q}_{f} \\
\mathbf{q}_{r}=0 \\
\mathbf{q}_{c}
\end{array}\right\},
$$

or

$$
\begin{equation*}
\mathbf{H} \boldsymbol{\phi}=\mathbf{G q} \tag{28}
\end{equation*}
$$

where $\boldsymbol{\phi}=\left\{\phi_{1}, \ldots, \phi_{N}\right\}^{\mathrm{T}}$ and $\mathbf{q}=\left\{\phi_{1, n}, \ldots, \phi_{N, n}\right\}^{\mathrm{T}}$. The elements of matrices $\mathbf{H}$ and $\mathbf{G}$ are respectively given by equations (23) and (24) with the constant $\alpha_{P}=0$.

### 3.1. SUB-DOMAINS AND THE CONTINUITY EQUATIONS FOR THE INTERFACES

If a baffle separates a liquid domain into two sub-domains (see Figure 2(b)), the system of equations (27) can be evaluated for each sub-domain as

$$
\begin{align*}
& {\left[\begin{array}{lllll}
\mathbf{H}_{f f I} & \mathbf{H}_{f r I} & \mathbf{H}_{f c I} & & \\
\mathbf{H}_{r f I} & \mathbf{H}_{r r I} & \mathbf{H}_{r c I} & & \\
\mathbf{H}_{c f I} & \mathbf{H}_{c r I} & \mathbf{H}_{c c I} & & \\
& & & \mathbf{H}_{c c I I} & \mathbf{H}_{c r I I} \\
& & \mathbf{H}_{r c I I} & \mathbf{H}_{r r I I}
\end{array}\right]\left\{\begin{array}{c}
\boldsymbol{\phi}_{f I} \\
\boldsymbol{\phi}_{r I} \\
\boldsymbol{\phi}_{c I} \\
\boldsymbol{\phi}_{c I I} \\
\boldsymbol{\phi}_{r I I}
\end{array}\right\}} \\
& \quad=\left[\begin{array}{llll}
\mathbf{G}_{f f I} & \mathbf{G}_{f r I} & \mathbf{G}_{f c I} \\
\mathbf{G}_{r f I} & \mathbf{G}_{r r I} & \mathbf{G}_{r c I} & \\
\mathbf{G}_{c f I} & \mathbf{G}_{c r I} & \mathbf{G}_{c c l} & \\
& & & \mathbf{G}_{c c I I}
\end{array}\right.  \tag{29}\\
& \mathbf{G}_{c r I I} \\
&
\end{align*}
$$

where subscripts $I$ and $I I$ denote the domains. In order to get a coupled system of equations, continuity conditions for the velocities and velocity potentials must be satisfied.

### 3.2. CONTINUITY CONDITIONS

Hydrodynamic pressures on each side of the interface of two separated domains should be equal. When liquids in the separated domains are identical, i.e., $\rho_{f I}=\rho_{f I I}$, the following continuity condition can be written:

$$
\begin{equation*}
\boldsymbol{\phi}_{c I}=\boldsymbol{\phi}_{c I I} . \tag{30}
\end{equation*}
$$

Here $c_{I}$ and $c_{I I}$ denote respectively the surfaces of the separated domains on the interface (see Figure 2(b)). Continuity of the velocity is satisfied by

$$
\begin{equation*}
\mathbf{q}_{c I}=-\mathbf{q}_{c I I} \tag{31}
\end{equation*}
$$

The coupled system of equations can be obtained by applying the continuity conditions on equation (29). After elimination of other unknowns, the following eigenvalue problem can be evaluated by using equation (14):

$$
\begin{equation*}
\mathbf{H}_{r e} \boldsymbol{\phi}_{f}=-\omega_{n}^{2} \mathbf{G}_{r e} \boldsymbol{\phi}_{f}, \tag{32}
\end{equation*}
$$

where components of $\boldsymbol{\phi}_{f}=\left\{\phi_{f f}, \ldots, \phi_{f N_{f}}\right\}^{\mathrm{T}}$ are the velocity potentials on the boundary elements of the free surface for the $n$th mode shape and the subscript re denotes reduced form. $N_{f}$ is the number of boundary elements on the free surface. Velocity potentials on the boundary elements on the rigid surfaces, $\phi_{r I}$ and $\phi_{\text {rII }}$, can be obtained by the back substitution of the evaluated velocity potentials.

## 4. NUMERICAL EXAMPLES

When the mode shapes and eigenfrequencies of equation (32) are calculated, the shear force and the overturning moment at the bottom of the tank, which are caused by the horizontal ground motion, can be determined. Duhamel's integral (19) is numerically evaluated by using the trapezoidal integration rule. The first 10 s of earthquake acceleration records with 0.01 s intervals has been used.

Only a few of the mode shapes corresponding to the smallest eigenfrequencies are required. The most effective modes, in response to the ground motion, correspond to the smallest eigenfrequencies, because of the fact that they always include most of the total energy of the system. In this study numerical examples were evaluated by using only the first two mode shapes. It has been checked numerically that these two modes provide sufficient accuracy.

All of the boundary elements are constant elements with the same length. On the free surface, for all examples, 10 constant boundary elements were used. On the other surfaces (wetted boundaries), the number of elements used depends on the ratios $R_{i} / R$ and $H / R$.

### 4.1. NATURAL VIBRATION ANALYSIS

### 4.1.1. Liquid in the cylindrical tank

The natural frequencies of the liquid in the cylindrical tank are given in Figure 4 for different ratios $H / R$ and for different radial wave numbers $n$. From Figure 4, it is seen that the natural frequency corresponding to the first mode reaches its limit value at about $H / R>1$, while the value for the second mode reaches its limit value at about $H / R>0.3$. Likewise, it is clear that the limits corresponding to the highest modes will occur at smaller ratios $H / R$.


Figure 4. Variation of natural frequencies ( $\cos \theta$ type) versus $H / R$.


Figure 5. Variation of natural frequencies ( $\cos \theta$ type) versus $R_{i} / R . H / R=1 ; h / H=0.3$.

When the internal radius of the baffle vanishes, the baffle separates the liquid domain into two domains. In this case, the liquid under the baffle behaves like a rigid solid and has no vibration, because it has no moving surfaces. Liquid in the upper domain has natural vibrations, because it has a free surface. Therefore, point 2 in Figure 5 for the cylindrical tank with a baffle ( $h / H=0 \cdot 3$ ) corresponds to point 2 in Figure 4 for the cylindrical tank without baffle $(H / R=0 \cdot 3)$. Similar situations are true for all of the points with the same numbers in the figures, because they denote identical situations in physical meaning.

### 4.1.2. Liquid in the cylindrical tank with a baffle

The natural frequencies are given in Figure 5, for $H / R=1$ and the tank with a baffle. From Figures 5 and 6, upon taking the circles with 1 and 4 into account, it is seen that the lower the depth of the baffle, the larger the effect of the baffle on the frequency.

### 4.2. SEISMIC analysis

The record which is used in the numerical examples, with 0.01 s intervals, belongs to the $N-S$ component of the 1992 Erzincan Earthquake, Turkey; see Figure 7. The acceleration values for the smaller intervals are obtained by using the linear interpolation method. The first 10 s of records has been used for all of the examples.

### 4.2.1. Liquid in the cylindrical tank

The maximum shear force and the overturning moment at the bottom of the tank without a baffle, for different values of $H / R$, are given in Figure 8. Some of the liquid, near to the base of the tall tank, has a rigid character like a solid. The rest has a behavior like a spring-mass system. A spring-mass system is the mechanical model of the sloshing part of the liquid [12, 15].


Figure 6. Variation of natural frequencies ( $\cos \theta$ type) versus $R_{i} / R . H / R=1 ; h / H=0 \cdot 1$.

### 4.2.2. Liquid in the cylindrical tank with a baffle

Any of the foundation forces can then be described by two components that are caused by the rigid part and the sloshing part. The liquid under the baffle behaves as a rigid part.

The rigid part causes larger shear force than the sloshing part. If the ratio $h / H$ decreases, the shear force at the bottom of the tank will increase (see Figure 9) and, in practice, the overturning moment will decrease (see Figure 10). If the inner radius of the baffle vanishes, the liquid inside the volume surrounded by the rigid surfaces behaves, of course, like a solid.

Points 7 and 8 in Figures $8-10$ show the values for a cylindrical tank without baffles. When the baffle is positioned as near as possible to the free surface of the liquid, it slightly affects the shear force and overturning moment at the bottom of the tank (see Figures 9 and 10).


Figure 7. Acceleration diagram: $N-S$ component of 1992 Erzincan Earthquake, Turkey.


Figure 8. Foundation forces at the bottom of the cylindrical tank versus $H / R$. (a) Shear force; (b) overturning moment.

## 5. CONCLUSIONS

The effectiveness of a baffle for damping liquid oscillations has been examined in an attempt to develop more efficient baffle configurations for seismic analysis of the tank. The baffles usually consist of rigid annular rings or plates which are fitted around the internal periphery of the tank.


Figure 9. Maximum shear force at the bottom of the tank, occurring in the first 10 s of the earthquake, versus $R_{i} / R . H / R=1$.


Figure 10. Maximum overturning moment at the bottom of the tank, occurring in the first 10 s of the earthquake, versus $R_{i} / R . H / R=1$.

For an effective passive control system, configurations can be designed by freely suspending baffles between limits along the tank wall and by positioning them slightly below the liquid surface. If stiffeners are required in the tank design for structural integrity, the baffles and support rings may serve the dual purpose of slosh damper and stiffener.

A baffle can be successfully used as a passive control system. For an effective passive control system, the inner radius should be greater than a half of the outer radius and the baffle should be located as near as possible to the free surface of the liquid. A baffle just on the free surface causes a non-linear behavior because of the unknown free surface. In this paper it has been assumed that the baffle is always surrounded by the liquid.

Although the baffle causes an increase in the value of the shear force (Table 1), it should be used to get a smaller overturning moment. The decrease in the ratio

## Table 1

The effects of the baffle on the foundation forces: (a) ratio of shear forces; (b) ratio of overturning moments

| $R_{i} / R d$ | $\overbrace{0.1}^{h / H}$ |  |
| :---: | :---: | :---: |
| 0.3 | (a) $F_{x}$ with $/ F_{x}$ without |  |
| 0.06 | 0.3 |  |
| 0.8 | (b) $M_{y}$ with $/ M_{y}$ without |  |
|  | 0.35 | 1.03 |
| 0.5 | 0.85 | 1.01 |
| 0.8 |  | 0.70 |

of overturning moments is strictly larger than the increase in the ratio of shear forces (see Table 1). This makes the usage of the baffle effective. As an example, for the location of the baffle such as $h / H=0 \cdot 1$ and inner radius $R_{i} / R d=0 \cdot 8$, shear force is increased $102 \%$ by the baffle. However the overturning moment is decreased $85 \%$ by the baffle.

The overturning moment can cause an uplift problem in the liquid storage tanks under the earthquake motion. Therefore, a baffle can be used to prevent this problem.

Other types of baffles, i.e., baffles capable of deflecting, deforming, and/or moving with respect to the tank wall will be the subject of the next study. In addition, the damping provided by rigid baffles of comparable size will be examined to determine the relative effectiveness between rigid and flexible systems. Furthermore, the subject of preventing uplift problems in liquid storage tanks under earthquake motion by using a baffle will also be a study in the future.

## REFERENCES

1. J. N. Yang, A. Danielians and S. C. Liu 1991 Journal of Engineering Mechanics, ASCE 117, 23704. A seismic hybrid control systems for building structures.
2. C. Y. Wang, Y. Tang, R. A. Uras, A. H. Marchertas, Y. W. Chang and R. W. Seidensticker 1991 Seismic Engineering, ASME 220, 13-22. Seismic response analysis of base isolated structures with high damping elastomeric bearings.
3. W. G. Vondorn 1966 Journal of Fluid Mechanics 24, 769-779. Boundary dissipation of oscillatory waves.
4. J. W. Miles 1958 Journal of Applied Mechanics 25, 274-276. Ring damping of free surface oscillations in a cylindrical tank.
5. R. D. Hanson 1973 National Academy of Sciences, 331-339. Washington, DC.
6. H. J. Epstein 1976 Journal of the Structural Division, ASCE 102, 1659-1673. Seismic design of liquid-storage tanks.
7. L. S. Jacobsen 1949 Bulletin of the Seismological Society of America 39, 189-204. Impulsive hydrodynamics of fluid inside a cylindrical tank and of fluid surrounding a cylindrical pier.
8. E. W. Graham and A. M. Rodriguez 1952 Journal of Applied Mechanics 19, 381388. The characteristics of fuel motion which affect airplane dynamics.
9. A. S. Veletsos 1974 Proceedings of the International Association for Earthquake Engineering Mechanics, Rome. Seismic effects in flexible liquid storage tanks.
10. A. S. Veletsos and Y. Tang 1987 Journal of the Engineering Mechanics Division, ASCE 113, 774-1792. Rocking response of liquid storage tanks.
11. W. Zhaolin, Q. Bin and C. Xuduo 1990 Acta Mechanica Sinica 8, 273-280. Viscoelastic plate fluid interactive vibration and liquid sloshing suppression.
12. V. Davidovici and A. Haddadi 1982 Annales de I'institut technique du batiment et des travaux publics $\mathbf{4 0 9}$. Calcul pratique de réservoirs en zone sismique.
13. J. W. Tedesco, C. N. Kostem and A. Kalnins 1987 Computers and Structures 26, 957-964. Free vibration analysis of cylindrical liquid storage tanks.
14. M. Utsumi, K. Kimura and M. Sakata 1987 The Japan Society of Mechanical Engineers 30, 467-475. The non-stationary random vibration of an elastic circular cylindrical liquid storage tank in simulated earthquake excitation.
15. D. D. Kana 1982 Nuclear Engineering and Design 69, 205-221. Status and research needs for prediction of seismic response liquid containers.
16. G. W. Housner 1957 Bulletin of the Seismological Society of America 47, 15-35. Dynamic pressures on the accelerated liquid containers.
17. G. W. Housner 1963 Bulletin of the Seismological Society of America 53, 381-387. The dynamic behavior of water tanks.
18. M. A. Haroun and G. W. Housner 1982 Journal of the Engineering Mechanics Division, ASCE EM5 108, 801-818. Complications in the free vibration analysis of tanks.
19. M. A. Haroun and G. W. Housner 1982 Journal of the Engineering Mechanics Division, ASCE EM5 108, 783-800. Dynamic characteristics of liquid storage tanks.
20. B. Hunt 1987 Journal of Engineering Mechanics, ASCE 113(5) (paper no. 21447), 653-670. Seismic-generated water waves in axisymmetric tanks.
21. M. Aslam, W. G. Godden and D. T. Scalise 1979 Journal of the Engineering Mechanics Division, ASCE EM3, 371-389. Earthquake sloshing in annular and cylindrical tanks.
22. B. Hunt and N. Priestley 1978 Bulletin of the Seismological Society of America 68, 487-499. Seismic water waves in a storage tank.
23. J. J. Stoker 1957 Water Waves. New York: Interscience Publishers. See section 2.1.
24. W. Wunderlich, H. Springer and W. Goebel 1989 IUTAM/IACM Symposium (editors H. A. Mang and G. Kuhn) Heidelberg, Vienna: Springer Verlag.
25. S. Uilhashi, H. Matsumoto, I. Nakahara and M. Shigeta 1987 The Japan Society of Mechanical Engineers 30, 568-573. Axisymmetrical impulsive response of an infinite circular cylindrical shell filled with liquid.
26. J. H. Hwang, I. S. Kim, Y. S. Seol, S. C. Lee and Y. K. Chon 1992 Computers and Structures 44, 339-342. Numerical simulation of liquid sloshing in three dimensional tanks.
27. M. Aslam 1981 International Journal for Numerical Methods in Engineering 17, 59170. Finite element analysis of earthquake induced sloshing in axisymmetric tanks.
28. C. Crawford 1965 Proceedings of the World Conference of Civil Engineers, New Zealand. Earthquake design loading for thin arch dams.
29. H. M. Westergatrd 1933 Transactions, ASCE 98, 418-433. Water pressures on dams during earthquakes.
30. R. G. Schwind, R. S. Scotti and S. Jörgen 1964 Report No. LMSC-A642961 (Contract No. NASI-4065), Lockheed Missiles and Space Co. The effect of the baffles on tank sloshing.
31. M. A. Silveria, D. G. Stephens and H. W. Leonard 1961 NASA TN-715. An experimental investigation of the damping of liquid oscillations in cylindrical tanks with various baffles.
32. J. A. Liggett and P. L.-F. Liu 1983 The Boundary Integral Equation Method for Porous Media Flow. London: George Allen \& Unwin.
33. A. Gedikli 1996 Ph.D. Thesis, Istanbul Technical University, Istanbul, Turkey. Fluid-structure interaction using variational BE-FE methods in cylindrical tanks.
